

# Effects of mesoscale gravity waves on sporadic E simulated by a one-dimensional dynamic model

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## Key Points:

- A one-dimensional dynamic model with low numerical dissipation is developed to simulate the evolution of sporadic E ( $E_s$ ) layers.
- Mesoscale gravity waves (GWs, periods <2 h) significantly affect the  $E_s$  layers above 100 km, but the effects are limited at lower altitudes.
- The effects of GWs on the  $E_s$  layers are complicated and include the reinforcement, diffusion, and driving of the wavelike vertical motion.

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**Abstract:** In addition to being driven by tidal winds, the sporadic E ( $E_s$ ) layers are modulated by gravity waves (GWs), although the effects are not yet comprehensively understood. In this article, we discuss the effects of mesoscale GWs on the  $E_s$  layers determined by using a newly developed model, MISE-1D (one-dimensional Model of Ionospheric Sporadic E), with low numerical dissipation and high resolution. Driven by the wind fields resolved by the high-resolution version of the Whole Atmosphere Community Climate Model with thermosphere and ionosphere extension (WACCM-X), the MISE-1D simulation revealed that GWs significantly influence the evolution of the  $E_s$  layer above 100 km but have a very limited effect at lower altitudes. The effects of GWs are diverse and complex, generally including the generation of fluctuating wavelike structures on the  $E_s$  layer with frequencies similar to those of the GWs. The mesoscale GWs can also cause increases in the density of  $E_s$  layers, or they can disperse or diffuse the  $E_s$  layers and increase their thickness. In addition, the presence of GWs is a key factor in sustaining the  $E_s$  layers in some cases.

**Keywords:** sporadic E; ion tidal layer; gravity waves; numerical simulation

## 1. Introduction

Sporadic E ( $E_s$ ) refers to the enhanced ionized layers at altitudes of ~95–130 km, which have frequently been observed by multiple measurements (e.g., Ogawa et al., 2002; Hysell et al., 2014; Yu BK et al., 2020). The presence of  $E_s$  layers in nature scatters radio propagation and thus has impacts on radio communication and modern navigation (Yue XA et al., 2016). A widely accepted view to explain the formation of  $E_s$  layers is the wind shear mechanism: the vertical shear of zonal and meridional winds causes long-lived ions (e.g., metallic ions) to converge (Haldoupis, 2011; Yamazaki et al., 2022; Qiu LH et al., 2023b). The zonal winds drive the ions across the geomagnetic fields and produce a vertical motion by the Lorentz force. The meridional winds drive ions along the

magnetic lines and generate vertical field-aligned transport. The variability of the neutral winds at the heights of  $E_s$  layers is mainly influenced by the atmospheric tides. Consequently, the  $E_s$  layers predominantly descend with the tidal nodes and are thus known as tidal ion layers (Mathews, 1998).

In addition to tidal winds, the atmospheric gravity waves (GWs) play a substantial role in the mesosphere and thermosphere. Although most GWs dissipate and deposit their momentum fluxes into the mean flow around the mesopause (~80 km), a spectrum of GWs still appears at the heights of the  $E_s$  layers (Lu X et al., 2009). These short-period fluctuations perturb the descending phase of the tides, thus producing complex effects on the  $E_s$  layers. Huang CS and Kelley (1996) predicted that the  $E_s$  layers will become a large-scale wavelike structure under the modulation of GWs. Gravity waves with short vertical wavelengths could shear out multiple  $E_s$  layers (Didebulidze et al., 2020). Short-term GWs with longer wavelengths, as presented by Qiu LH et al. (2023a), can also significantly affect the  $E_s$  layers. The ion density may increase more than twofold, or the  $E_s$  layers may disperse or even

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disappear. Those works gave us the first glimpse of how the GWs influence the  $E_s$  evolution. However, from the simulation perspective, many issues still need to be improved. The priority is that the numerical scheme needs to satisfy the requirement for dealing with the dynamic processes in the fine grids. To simulate such a thin thickness of  $E_s$  layers, the model should have better conservation and less dissipation. Otherwise, the numerical scheme will additionally introduce spurious diffusion. Although the presence of diffusion in nature is important to prevent the  $E_s$  layer from becoming too thin, the spurious diffusion attributable to the numerical scheme could lead to overestimation of the dispersion effect of GWs on the  $E_s$  layers or could provide additional ions for GWs to shear out secondary  $E_s$  layers above or below the peaks. Moreover, the mesoscale GWs induce dramatic changes in the vertical wind shear, so this fact requires robust model stability to handle the rapid changes of inflow and outflow on the grids. In this work, we develop a novel one-dimensional Model of Ionospheric Sporadic E (MISE-1D), which solves the dynamic processes in the evolution of  $E_s$  with low numerical dissipation and has strong stability.

To investigate the effects of mesoscale GWs (periods  $< 2$  h) on the  $E_s$  layers, a series of numerical experiments are performed under conditions with and without GWs. The specified neutral winds, including the resolved mesoscale GWs, are provided by the high-resolution version of the Whole Atmosphere Community Climate Model with thermosphere and ionosphere extension (WACCM-X; Liu HL et al., 2023, 2024). In the first step, we exclude physical diffusion to examine whether the GWs facilitate the diffusion of  $E_s$  layers or have other influences. In the next step, the ambipolar diffusion is introduced, and the aim is to investigate how strong the GW effects are compared with the ambipolar diffusion. Because the strength of GWs depends on the latitudes (Hoffmann et al., 2013; Miyoshi et al., 2014), we select two typical locations at mid- and low latitudes in China, Mohe (53.5°N, 122.3°E) and Sanya (18.3°N, 109.6°E). The selection of location also considers that the two sites have established a new lidar and a new incoherent scatter radar, respectively, both of which can measure the  $E_s$  layers with high spatiotemporal resolution (Yue XA et al., 2022a, 2022b; Zhou X et al., 2023; Chen FL et al., 2024). Our simulation work should therefore be a very useful complement to future observations.

This article is organized as follows: The MISE-1D is introduced in Section 2, including the numerical scheme and specific settings. The effects of mesoscale GWs on the evolution of  $E_s$  layers are presented in Section 3. Section 4 discusses the advantages and disadvantages of the present work and gives a brief perspective of future studies. A summary is given at the end.

## 2. Model Description

### 2.1 Numerical Scheme

The  $E_s$  layers are formed by wind shear, so the dynamic calculation is the most important issue. In this work, we adopt a numerical scheme that has low diffusion, which has been applied to the simulation of ionospheric spread F (Li ZZ et al., 2021, 2023) and the magnetosphere (Zhang BZ et al., 2019). The MISE-1D numerically solves the continuous equation of ions by the finite-volume method, which has better conservation than the finite-difference

method. Given that the electrons are strongly magnetized at the heights of the  $E_s$  layers, the plasma motion is equal to the ion motion, and electrons follow the ions by Coulomb force to maintain plasma neutrality. The integral form of the governing equation can then be expressed as

$$\frac{\partial}{\partial t} \oint N_i dV = - \oint F_i dS, \quad (1)$$

where  $N_i$  is the density of the metallic ion,  $dV$  is the control volume, and  $dS$  is the surface area. The total fluxes  $F_i = C_i + D_i$  comprise the convection attributable to vertical ion motion ( $C_i = N_i w_i$ ) and diffusion ( $D_i$ ), both of which are defined as positive in the outflowing direction of the interface surface. The production and loss terms (e.g., chemical recombination or metallic influx from space) are neglected in this dynamic model. In this one-dimensional model, the influx and outflux in the horizontal direction are ignored. Changes in number density in a time step can then be discretized as

$$N_j^{n+1} - N_j^n = - \frac{\Delta t}{\Delta h} \left( F_{j+1/2}^{n+1/2} - F_{j-1/2}^{n+1/2} \right), \quad (2)$$

where we discard the subscript  $i$  because both number density and fluxes are referred to as ions. The replaced subscript  $j$  indicates the  $j$ th grid vertically, and superscript  $n$  means the  $n$ th time step. The time step ( $\Delta t$ ) is not set to be a constant but depends on the Courant–Friedrichs–Lewy condition (CFL) condition. A CFL value ( $w_i \Delta t / \Delta h$ ) less than 0.25 is safe to ensure the model stability for the convection calculation. As shown in Equation (3), the corrector step is calculated after a predictor step ( $F^{n+1/2}$ ), which is given by the Adams–Bashforth scheme with third-order accuracy:

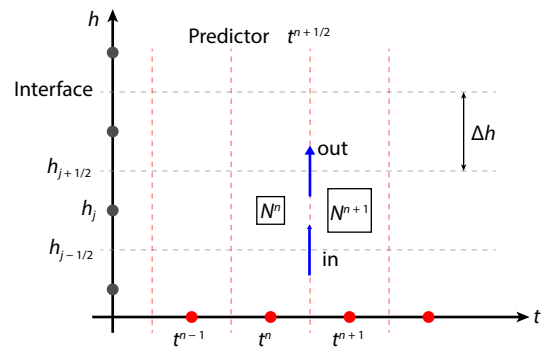
$$F^{n+1/2} = \frac{15}{8} F^n - \frac{5}{4} F^{n-1} + \frac{3}{8} F^{n-2}. \quad (3)$$

Figure 1 schematically illustrates the procedures in the dynamic calculation of the MISE-1D model.

#### 2.1.1 Convection

To solve the convection, the flux values at  $j + 1/2$  interfaces are reconstructed according to the seventh upwind scheme (Zhang BZ et al., 2019):

$$C_{j+1/2}^1 = -\frac{1}{140} C_{j-3} + \frac{5}{84} C_{j-2} - \frac{101}{420} C_{j-1} + \frac{319}{420} C_j + \frac{107}{420} C_{j+1} - \frac{19}{210} C_{j+2} + \frac{1}{105} C_{j+3}. \quad (4)$$



**Figure 1.** Schematic diagram of the numerical calculation procedures in the MISE-1D.

The flux values on the left and right sides utilize the same reconstruction coefficients by switching only the upwind direction. In addition, the limiter with the partial donor cell method is applied to monitor discontinuities. If the sharp discontinuities are captured, the limited values will be set to guarantee no overshooting or undershooting. The effective ion motion in vertical ( $w_i$ ) is driven by the neutral winds, characterized as

$$w_i = \frac{v_{in}\omega_i}{\omega_i^2 + v_{in}^2} U \cos l - \frac{\omega_i^2}{\omega_i^2 + v_{in}^2} V \cos l \sin l = f_u U - f_v V, \quad (5)$$

where  $v_{in}$  and  $\omega_i$  are the ion-neutral collision frequency and gyrofrequency, respectively. The ion-ion and ion-electron collisions are ignored because of their small values in the region of interest. The calculation of the ion-neutral collision frequency requires information on the neutral temperature and the densities of nonmetallic species (e.g., O, O<sub>2</sub>, N<sub>2</sub>, NO), which, in this work, are provided by the NRLMSIS-00 model (Picone et al., 2002). The geomagnetic inclination  $l$  is given by the International Geomagnetic Reference Field (IGRF)-12 model (Thébault et al., 2015). The layer-forming efficiencies of zonal and meridional wind shear ( $f_{u,v}$ ) are then calculated. The positive directions of zonal ( $U$ ) and meridional ( $V$ ) winds are eastward and northward, respectively. The effects of electric fields are not considered at present.

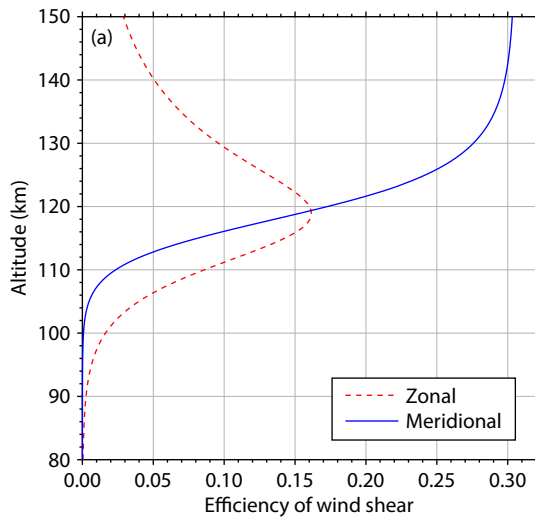
### 2.1.2 Diffusion

The metallic ions are the main constituents in the E<sub>s</sub> layer, so they can be considered the major species. Although the molecular ions are also dominant in the daytime, the density of long-lived metallic ions is still large. The physical diffusion of major ion species in the vertical dimension is dominated by the ambipolar diffusion (Schunk and Nagy, 2009), which is written as

$$D_i = -\Gamma_a \left[ \frac{\partial N_i}{\partial z} + \frac{N_i}{T_i + T_e} \frac{\partial (T_i + T_e)}{\partial z} - \frac{N_i m_i g \sin l}{k_B (T_i + T_e)} \right] \sin l, \quad (6)$$

where the ambipolar diffusion coefficient is given by

$$\Gamma_a = \frac{k_B (T_i + T_e)}{m_i v_{in}}. \quad (7)$$



The ion, electron, and neutral temperatures are assumed to be the same in this model ( $T_e \approx T_i \approx T$ ) because of the sufficient heat exchanges between them in the E region. The calculation of the ion-neutral collision frequency ( $v_{in}$ ) adopts the formula in the SAMI3 (Sami3 is A Model of the Ionosphere) model (Huba et al., 2019). The  $k_B$  is the Boltzmann constant, and  $m_i$  is the ion mass density. Because the ambipolar diffusion is along the magnetic lines, the vertical motion attributable to diffusion should multiply the term of  $\sin l$ . The discretization of ambipolar diffusion adopts an explicit scheme on the gradient terms based on the central difference method. The influx and outflux are calculated at the  $j \pm 1/2$  interfaces of the predictor step. For example, changes in the density at the  $j$ th grid point caused by the diffusion of density gradients from time step  $n$  to time step  $n + 1$  are written as

$$\frac{\Delta t}{\Delta h^2} \left[ \Gamma_{a,j+\frac{1}{2}}^{n+\frac{1}{2}} \left( N_{j+1}^{n+\frac{1}{2}} - N_j^{n+\frac{1}{2}} \right) - \Gamma_{a,j-\frac{1}{2}}^{n+\frac{1}{2}} \left( N_j^{n+\frac{1}{2}} - N_{j-1}^{n+\frac{1}{2}} \right) \right]. \quad (8)$$

Notably, to satisfy the stability requirement, the time step  $\Delta t$  in the diffusion calculation should at least be smaller than  $\Delta h^2 / 2\Gamma_a$ .

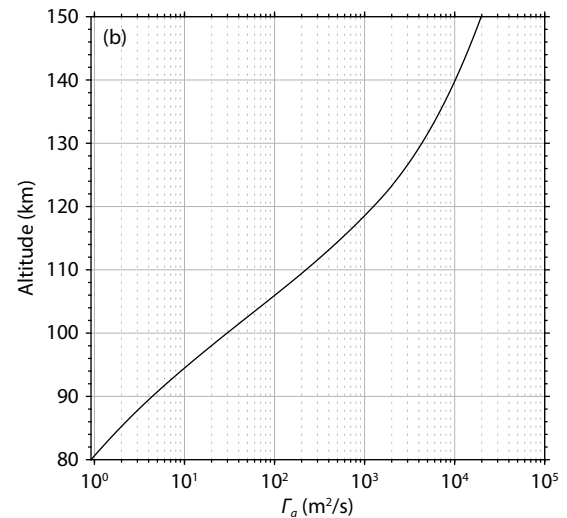
## 2.2 Model Settings

In this work, we choose the magnesium ion (Mg<sup>+</sup>) for simulation, which is one of the most dominant metallic species in E<sub>s</sub> layers. The initial profile of Mg<sup>+</sup> is given by the formula of Langowski et al. (2015):

$$N_{Mg^+} = \begin{cases} 10^9 \times \exp \left[ -\frac{(h-97)^2}{60} \right] & (h < 97 \text{ km}) \\ 10^9 \times \exp \left[ -\frac{(h-97)^2}{250} \right] & (h \geq 97 \text{ km}) \end{cases}, \quad (9)$$

where  $N_{Mg^+}$  is in m<sup>-3</sup>,  $h$  is the altitude in units of kilometers.

The Mg<sup>+</sup> layer-forming efficiencies of zonal and meridional wind shear ( $f_{u,v}$ ), which is mentioned in Equation (5), at the Mohe location are shown in Figure 2a. For the Mg<sup>+</sup> convergence, the meridional wind shear is more important than the zonal wind shear above ~120 km, and it increases with altitude. The zonal wind shear has



**Figure 2.** (a) Vertical profiles of Mg<sup>+</sup> layer-forming efficiencies of zonal (red dashed line) and meridional (blue solid line) wind shear. (b) Ambipolar diffusion coefficients of Mg<sup>+</sup> estimated as a function of altitude.

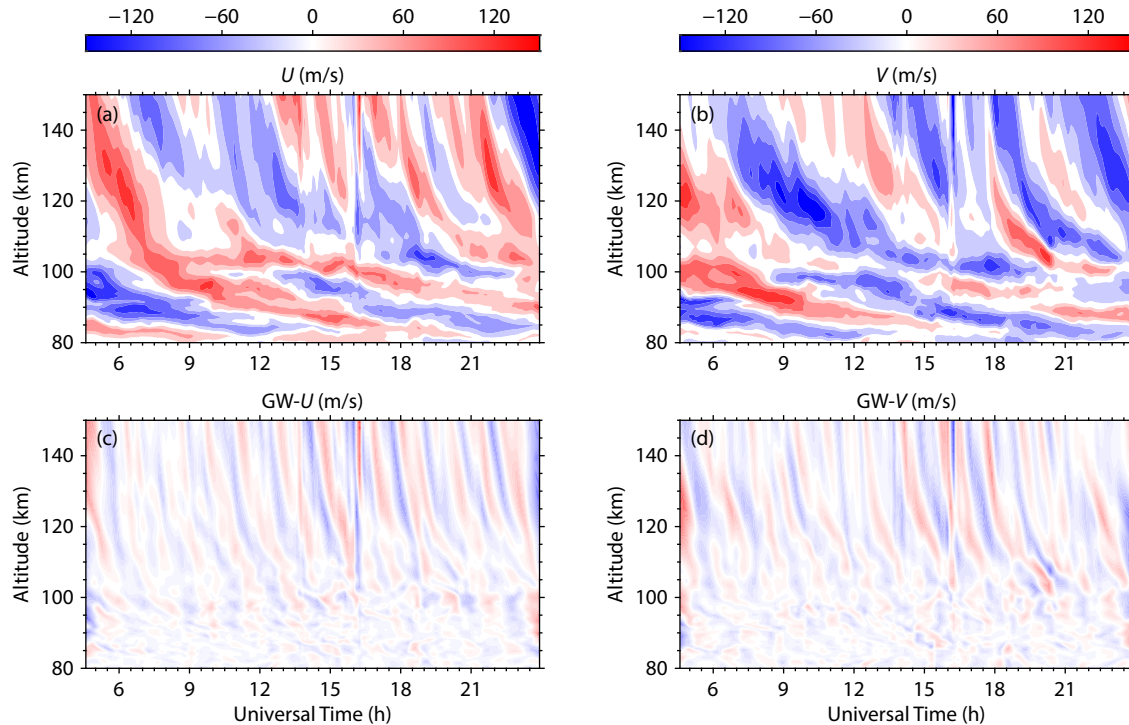
greater efficiency than the meridional wind shear below  $\sim 120$  km, reaching a peak value of  $\sim 0.16$ . As for the ambipolar diffusion, the coefficients increase exponentially from  $30 \text{ m}^2/\text{s}$  at  $100$  km to  $\sim 20,000 \text{ m}^2/\text{s}$  at  $150$  km (Figure 2b). This indicates that the diffusion in the upper E region is much stronger than that in the lower E region. We therefore set the height of the upper boundary at  $150$  km, rather than much higher, considering that the larger  $\Gamma_a$  at higher altitudes requires the time step to be extremely small.

Neutral winds are specified by the high-resolution version of the WACCM-X model (Liu HL et al., 2023), whose aim is to simulate the influences of the Hunga Tonga volcanic eruption in the atmosphere and ionosphere. The temporal resolution is  $5$  min and the vertical resolution at the height of  $E_s$  layers is  $\sim 0.6\text{--}2.0$  km, so the model is able to capture the characteristics of mesoscale GWs (Liu HL et al., 2024). Figures 3a–3b show the resolved wind fields over Mohe ( $53.5^\circ\text{N}$ ,  $122.3^\circ\text{E}$ ) at heights of  $80\text{--}150$  km. The semidiurnal tides are dominant at  $80\text{--}100$  km with a vertical wavelength of  $\sim 20$  km. Gravity waves with smaller periods become much more important above  $100$  km. The mesoscale GWs are retrieved by high-pass filtering with a cutoff period of  $2$  h and are shown in Figures 3c–3d. The apparent period of the resolved mesoscale GWs is approximately  $1.5$  h, and the magnitude can reach  $\pm 50$  m/s in the lower thermosphere ( $\sim 100\text{--}150$  km). The vertical wavelength of GWs above  $100$  km is approximately  $30$  km, and it increases with height. The wavefront of an apparent Lamb mode, which was generated by the Hunga Tonga volcanic eruption, reaches Mohe at approximately  $16:00$  universal time (UT), with a period of less than one hour. As for the horizontal winds over Sanya (Figure 4), diurnal tides dominate below  $100$  km, and semidiurnal tides become strong above  $100$  km. The amplitudes of GWs reach  $\sim 20$  m/s, which are smaller than those at Mohe. The arrival time of

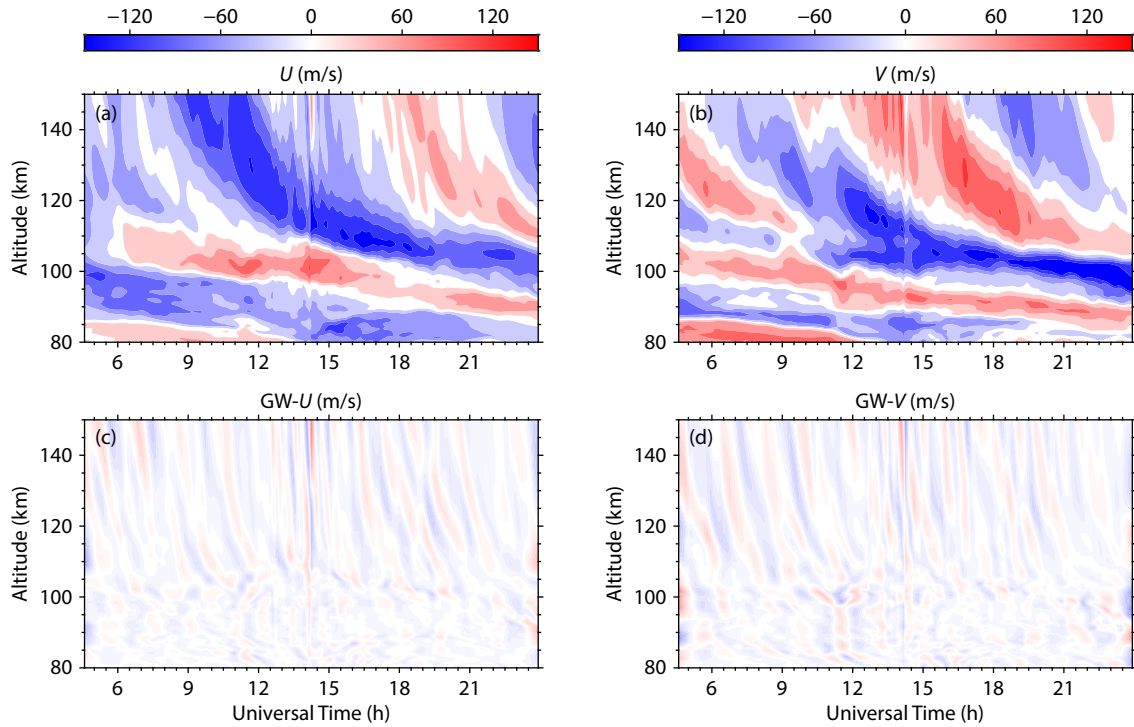
the Lamb wave is  $\sim 14:00$  UT, about  $2$  h earlier than that reaching Mohe.

### 3. Simulation Results

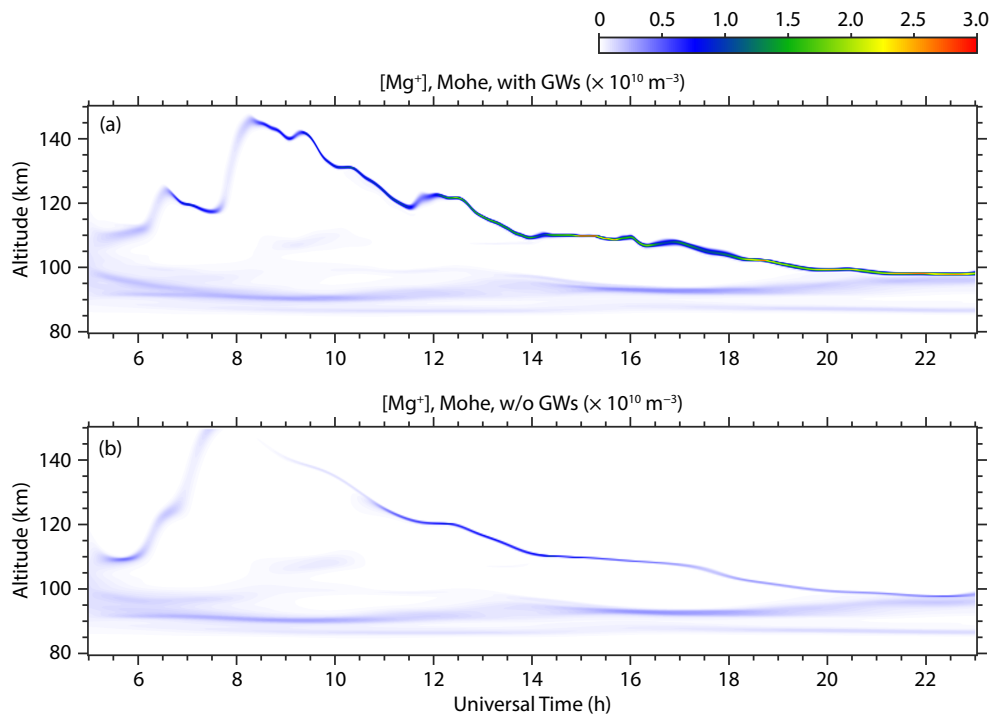
First, we examine the evolution of the  $\text{Mg}^+$  density over Mohe simulated by the MISE-1D model, without the physical diffusion (Figure 5). Figures 5a–5b illustrate the results driven by the wind fields with and without the mesoscale GWs, respectively. The  $E_s$  layers above  $100$  km are thin in both the absence and presence of GWs, resulting from the exclusion of the diffusion term. The GWs mainly affect the  $E_s$  layers above  $100$  km, whereas their effects are much more limited below that. One of the most obvious effects is the short-period up-and-down motion. For instance, when the GWs are included, the peak height of the  $E_s$  layer decreases significantly from approximately  $06:30$  to  $07:30$  UT and fluctuates as the Lamb wave approaches ( $\sim 16:00$  UT). Another important influence is the strength of the  $E_s$  layer. The number density in the  $E_s$  layer above  $100$  km is much larger in the case with GWs than in the case without GWs. The GWs can also induce periodic changes in the  $E_s$  strength, which is strong at approximately  $18:40$ ,  $20:10$ , and  $21:40$  UT. The time interval is similar to the wind period shown in Figure 3. In addition, GWs play a role in diffusing the  $E_s$  layer. The thin  $E_s$  layer begins to diffuse at  $\sim 120$  km around  $11:30$  UT in the presence of GWs, whereas the  $E_s$  layer remains narrow at this time in the absence of GWs. Figure 6 further illustrates how the GWs disperse the  $E_s$  layer. The presence of GWs causes additional vertical wind shear in both the zonal and meridional winds, and the net effect is to induce additional upward ion motion above  $120$  km and downward ion motion below it. The different ion velocities at the interface of  $120$  km disperse the converged ion layer, and the net behavior is like diffusion. In this case, the full width at half maximum



**Figure 3.** The (a) zonal ( $U$ ) and (b) meridional ( $V$ ) winds simulated by the high-resolution WACCM-X model on January 15, 2022, over Mohe ( $53.5^\circ\text{N}$ ,  $122.3^\circ\text{E}$ ). Mesoscale gravity waves (GW; periods  $< 2$  h) are filtered from the simulated winds, as illustrated in plots (c) and (d).



**Figure 4.** Same as Figure 3, but for the Sanya location (18.3°N, 109.6°E).



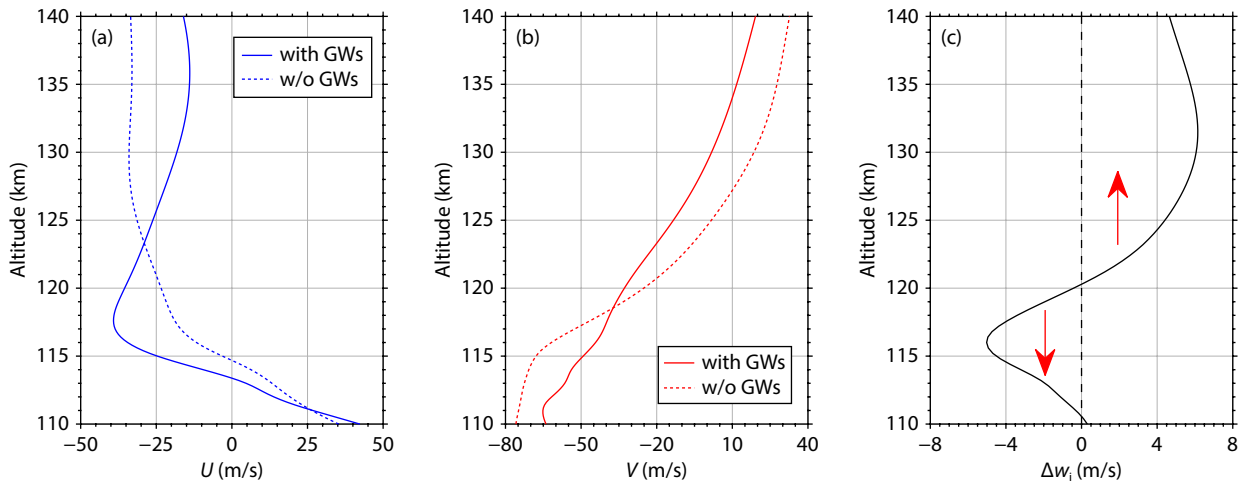
**Figure 5.** Temporal evolution of number density of  $\text{Mg}^+$  (a) with and (b) without (abbreviated as w/o) the mesoscale GWs simulated under nondiffusion conditions.

(FWHM) of the  $E_s$  layer increases from  $\sim 0.8$  to  $\sim 2.4$  km because of the presence of GWs. In particular, the effects of GWs on  $E_s$  evolution are apparently complex, involving periodic up-and-down motions, an increase in density, and the diffusion of the  $E_s$  layers.

The ambipolar diffusion is then included in the MISE-1D simulation (Figure 7). The  $\text{Mg}^+$  density is generally much lower and the thick-

ness of the  $E_s$  layers is larger than that without diffusion (Figure 5), especially above 120 km, where the diffusion coefficient becomes large. The MISE-1D model captures the reasonable FWHM of the  $E_s$  layers ( $\sim 1$ – $5$  km), which is comparable with that in the observation (Qiu LH et al., 2021). The effects of GWs on the  $E_s$  layers are similar to those without ambipolar diffusion, which also manifests



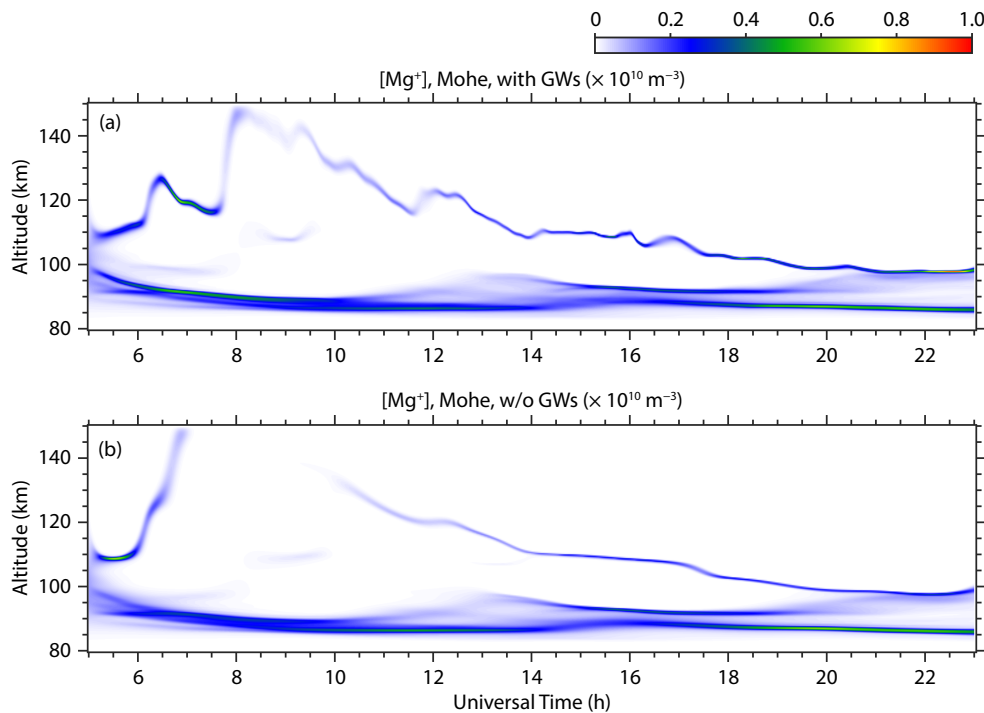


**Figure 6.** Vertical profiles of (a) zonal ( $U$ ) and (b) meridional ( $V$ ) winds in the presence (solid lines) and absence (dotted lines) of mesoscale GWs, at 11:30 UT. The corresponding differences in gyrofrequency ( $w_i$ ) are plotted in panel (c), where red arrows indicate the direction of ion motion attributable to the GW effects.

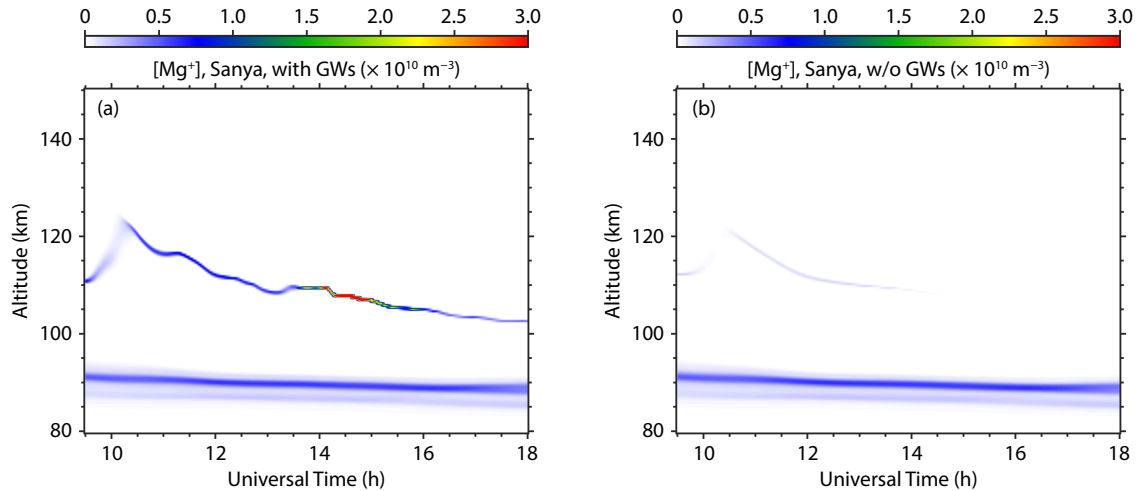
as an up-and-down fluctuation, reinforcement, and dispersion of the  $E_s$  layers. However, in contrast to the report by Didebulidze et al. (2020), no significant multilayer effect is observed. This may be partly because the WACCM-X resolved the wavelength of mesoscale GWs in the lower thermosphere as larger than that specified by Didebulidze et al. (2020). Although the wavelengths of GWs below 100 km in this work are similar to those in their work, the GW effects at these altitudes in our simulation are still nonsignificant. In addition, the GWs in this case can generate a similar magnitude of dispersion on  $E_s$  layers compared with ambipolar diffusion, for example, around 11:50 and 16:40 UT.

In addition, Figure 8 shows the simulation results at Sanya without

the consideration of ambipolar diffusion. This plot is intended to illustrate the effects of GWs alone rather than as a comparison between the effects of GWs and ambipolar diffusion. In the absence of GWs, the intensity of the  $E_s$  layer above 100 km is much weaker than that over Mohe and even disappears after 14:00 UT, although the vertical wind shear is also very strong (Figure 4). This result is consistent with our intuition because the geomagnetic inclination at Sanya is relatively small ( $\sim 25.7^\circ$ ), which prevents the ions from converging vertically. As a result, the occurrence of the  $E_s$  layer at low latitudes is much smaller than that at mid-latitudes (Yu BK et al., 2019; Liu Y., 2021). However, once the GWs are included, the  $E_s$  layer over Sanya becomes as strong as that over Mohe. With the arrival of the Lamb wave



**Figure 7.** Same as Figure 5, but with consideration of the ambipolar diffusion.



**Figure 8.** The evolution of  $E_s$  layers over Sanya in the (a) presence and (b) absence of mesoscale GWs without the ambipolar diffusion.

around 14:00 UT, the  $E_s$  layer is significantly strengthened and continuously maintained. The GWs also affect the  $E_s$  layer over Sanya similar to that over Mohe, for example, by generating fluctuation and increasing its thickness. But in this case, the mesoscale GWs are also a key factor in maintaining the  $E_s$  layer.

#### 4. Discussion

One of the advantages of this work is the numerical scheme in the convection calculation, which has low dissipation and can simulate rapid changes in the evolution of the  $E_s$  layer with high resolution. Low dissipation is also advantageous for discussing the GW diffusion effect compared with physical diffusion in nature. Physical diffusion is crucial for the evolution of  $E_s$  layers, especially in the upper E region, where ion-neutral collisions decrease. The presence of physical diffusion prevents the  $E_s$  layer from becoming too narrow and maintains a thickness of approximately 1–5 km (Qiu LH et al., 2021). In addition, physical diffusion is thought to contribute to the disappearance of the  $E_s$  layers (Earle et al., 2000). Neglecting the physical diffusion term has been a common treatment in previous simulation studies, and their models have still been able to simulate  $E_s$  layers with a reasonable thickness (e.g., Zuo XM et al., 2006; Carrasco et al., 2007). Ignoring physical diffusion has generally not been very problematic because the numerical schemes generally introduce additional numerical dissipation, which is actually helpful in maintaining model stability. The numerical dissipation also acts as spurious diffusion to spread the  $E_s$  layers and prevent the layers from becoming too thin. However, numerical dissipation mostly depends on the calculation scheme, whereas diffusion in nature varies with height. When we discuss the possible roles of GWs in the diffusion or dispersion of  $E_s$  layers, the conventional treatment in the numerical scheme needs to be reconsidered, and adoption of a scheme with low numerical dissipation is necessary.

We found that the mesoscale GWs could dynamically disperse the  $E_s$  layers as strongly as the physical ambipolar diffusion, benefiting from the numerical consideration. When the vertical shear of the GWs induced the parting motion around the  $E_s$  peaks in the opposite direction, the  $E_s$  layer would disperse and the thickness would become greater. However, the effect of the dynamic diffusion

mechanism on the terrestrial  $E_s$  layers would not produce the  $E_s$  “rifts” similar to those constantly observed on Mars (Collinson et al., 2020). In our simulation, the GWs did not form multiple  $E_s$  layers, as reported by Didebulidze et al. (2020). The compelling reason for this difference is that the wavelength they artificially specified was as short as 15 km, whereas the WACCM-X resolved the wavelength of GWs in the  $E_s$  heights as being larger than 30 km above 100 km. Although ambipolar diffusion was involved, the GWs still did not shear additional  $E_s$  layers. Moreover, the GW wavelengths in the simulation by Qiu LH et al. (2023a) were quite large, and they also did not find multiple layering effects.

The MISE-1D at the current stage is a simple convection–diffusion model. The consideration of GW influences in this work is only from a dynamical perspective, and chemical reactions and electric fields are not considered, some aspects of which are also important (Andoh et al., 2022, 2023). It would be worthwhile to include these processes and develop a three-dimensional framework in future research. In addition, with the progress of observations, fine structures inside the  $E_s$  layer have gradually been revealed (e.g., Hysell et al., 2013; Ejiri et al., 2019; Jiao J et al., 2022). These small-scale structures are thought to be associated with plasma instabilities, such as the Kelvin–Helmholtz instability (e.g., Larsen, 2000; Bernhardt, 2002), the gradient-drift instability (Woodman et al., 1991), and the GW-driven plasma instability (Shalimov et al., 2009). Some simulation work has resulted in preliminary discussions of these nonlinear processes (e.g., Cosgrove and Tsunoda, 2003; Wu JN et al., 2022), and more extensive discussions coupling advanced simulations and observations would deepen our understanding.

#### 5. Conclusions

In this work, we developed a novel dynamic model, MISE-1D, to simulate the effects of GWs on the evolution of  $E_s$  layers. The model calculated the metallic-ion motion in the vertical direction based on the finite-volume method, with careful consideration of the numerical dissipation. Neutral winds simulated by the high-resolution version of WACCM-X were then specified in the model, and the effects of mesoscale GWs (periods <2 h) were evaluated. When the simulation results with and without the mesoscale GWs were compared, the effects of GWs on the  $E_s$  layers were revealed

and were found to be significant above 100 km. These effects were generally diverse and complicated for both the Mohe and Sanya sites. Such effects included the generation of wavelike fluctuations, the enhancement of strength, and the dispersion of  $E_s$  layer thickness. This dynamic dispersion effect is comparable with ambipolar diffusion at  $\sim 120$  km. The presence of GWs can also be a critical factor in maintaining the  $E_s$  layers in certain cases.

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